## Mathematical Methods for Computer Science II

Spring 2021

Series 7 – Hand in before Monday, 26.04.2021 - 12.00

1. Construct a DFA equivalent to the  $\varepsilon$ -NFA given by the following table.

	ε	a	b	c
$q_0$	$\{q_1, q_2\}$	Ø	$\{q_1\}$	$\{q_2\}$
$q_1$	Ø	$\{q_0\}$	$\{q_2\}$	$\{q_0,q_1\}$
$q_2$	Ø	Ø	Ø	Ø

The initial state is  $q_0$ , the only final state is  $q_2$ .

- 2. a) Construct an  $\varepsilon$ -NFA for the set of binary words consisting either of repeating 01 or of repeating 010 (the empty word  $\varepsilon$  also belongs to this language).
  - b) Construct a finite automaton (DFA, or NFA, or  $\varepsilon$ -NFA) for the set of binary words which contain at least one symbol 1 in the last three positions. Try to minimize your construction.
- 3. Describe the following languages in a human language as briefly as possible. a)  $(0^*1^*)^*$ 
  - b)  $(0+1)^*0(0+1)^*0(0+1)^*$
  - c)  $(1^*01^*01^*)^*$
  - d)  $(1+01)^*$
- 4. Find regular expressions for the following languages.
  - a) Sequences of zeros of length n such that n dollars can be changed into bills of 17 and 31 dollars.
  - b) Binary words with two consecutive 1s at some place.
  - c) Binary words without two consecutive 1s.
  - d) Binary words whose number of 0s is odd.
- 5. Show that for every  $\varepsilon$ -NFA with *n* states and at least one  $\varepsilon$ -transition there is an equivalent DFA with at most  $3 \cdot 2^{n-2}$  states.